

Speaker: Frank Schäfer

Title: Replacing neural networks by optimal analytical predictors for the detection of phase transitions

Place: Seminar room (915)

Abstract:

Identifying phase transitions and classifying phases of matter is central to understanding the properties and behavior of a broad range of material systems. In recent years, machine-learning (ML) techniques have been successfully applied to perform such tasks in a data-driven manner. However, the success of this approach notwithstanding, we still lack a clear understanding of ML methods for detecting phase transitions, particularly of those that utilize neural networks (NNs). In this talk, we present analytical expressions derived for the optimal output of three widely used NN-based methods for detecting phase transitions [1]. These optimal predictions correspond to the results obtained in the limit of high model capacity. Therefore, they can be recovered, for example, using sufficiently large, well-trained NNs. The inner workings of the considered methods are revealed through the explicit dependence of the optimal output on the input data. By evaluating the analytical expressions, we can identify phase transitions directly from experimentally accessible data without training NNs, which makes this procedure favorable in terms of computation time. Our theoretical results are supported by extensive numerical simulations covering, e.g., topological, quantum, and many-body localization phase transitions. We expect similar analyses to provide a deeper understanding of other classification tasks in condensed matter physics.

[1] Julian Arnold and Frank Schäfer, *Phys. Rev. X* 12, 031044 (2022).